

## AQA 8300 GCSE Foundation Mathematics: Checklist

### Number

order positive and negative integers, decimals and fractions	
use the symbols =, ≠, <, >, ≤, ≥	
apply +, -, × and ÷ to integers, decimals and simple fractions (proper and improper), and mixed numbers – all both positive and negative	
understand and use place value	
recognise and use relationships between operations, including inverse operations (e.g. cancellation to simplify calculations and expressions)	
be able to use order of operations, including brackets, powers, roots and reciprocals (BIDMAS)	
know and be able to find the following: prime numbers, factors (divisors), multiples, HCF, LCM, prime factorisation, including using product notation and the unique factorisation theorem	
apply systematic listing strategies	
use positive integer powers and associated real roots (squares up to $15 \times 15$ , cube and higher), recognise powers of 2, 3, 4, 5	
Know that $1000 = 10^3$ and 1 million = $10^6$	
Calculate with roots and with integer powers	
Give exact answers as fractions and/or multiples of $\pi$	
Identify a number that is in standard form and be able to calculate with it	
work interchangeably with terminating decimals and their corresponding fractions (such as 3.5 and $\frac{7}{2}$ or 0.375 and $\frac{3}{8}$ )	
identify and work with fractions in ratio problems	
interpret fractions and percentages as operators	
use standard units of mass, length, time, money and other measures (including standard compound measures)	
know and use metric conversion factors for length, area, volume and capacity.	
estimate answers	
check calculations using approximation and estimation, including answers obtained using technology (mainly calculators)	
round numbers and measures to an appropriate degree of accuracy (e.g. to a specified number of decimal places or significant figures)	
specify error intervals using inequalities e.g. $4.5 \leq x < 5.5$	
understand not to round values unless it is the final answer	
apply and interpret limits of accuracy e.g. to the nearest cm.	

### Algebra

use and interpret algebraic notation, including:	
<ul style="list-style-type: none"> <li>• ab in place of <math>a \times b</math></li> <li>• <math>3y</math> in place of <math>y + y + y</math> and <math>3 \times y</math></li> <li>• <math>a^2</math> in place of <math>a \times a</math>, <math>a^3</math> in place of <math>a \times a \times a</math>, <math>a^2b</math> in place of <math>a \times a \times b</math></li> <li>• <math>\frac{a}{b}</math> in place of <math>a \div b</math></li> <li>• coefficients written as fractions rather than as decimals</li> <li>• brackets</li> </ul>	
substitute numerical values into formulae and expressions	
know and be able to identify the following: expressions, equations, formulae, inequalities, terms and factors	
simplify and manipulate algebraic expressions (including those involving surds) by:	
<ul style="list-style-type: none"> <li>• collecting like terms</li> <li>• multiplying a single term over a bracket</li> <li>• taking out common factors</li> <li>• simplifying expressions involving sums, products and powers, including the laws of indices</li> <li>• expanding two brackets</li> <li>• factorising quadratic expressions, including the difference of two squares</li> </ul>	
understand and use standard mathematical formulae e.g. $A = \pi r^2$	
be able to change the subject of a formulae	
know the difference between an equation and an identity	
argue mathematically to show algebraic expressions are equivalent, and use algebra to support and construct arguments	
where appropriate, interpret simple expressions as functions with inputs and outputs	
work with coordinates in all four quadrants	
plot graphs of equations that correspond to straight-line graphs in the coordinate plane	
use the form $y = mx + c$ to identify parallel lines	
find the equation of the line through two given points, or through one point with a given gradient	
identify and interpret gradients and intercepts of linear functions graphically and algebraically	
identify and interpret roots, intercepts and turning points of quadratic functions graphically - find roots algebraically	
recognise, sketch and interpret graphs of linear functions and quadratic functions, including simple cubic functions and the reciprocal function $y = \frac{1}{x}$ with $x \neq 0$	
plot and interpret graphs, and graphs of non-standard functions in real life contexts	
find approximate solutions to problems such as simple kinematic problems involving speed-distance-time and acceleration-time graphs including reciprocal graphs	
solve linear equations in one unknown, including those with the unknown on both sides of the equation and those with brackets	
find approximate solutions to an equation using a graph	
solve quadratic equations algebraically by factorising and find approximate solutions using a graph	
be able to form and solve expressions from a given situation	
be able to form an equation (or two simultaneous equations), solve the equation(s) and interpret the solution	

solve linear inequalities in one variable and represent the solution set on a number line	
generate future terms of a sequence using a term-to-term rule or the nth term	
recognise and use sequences of triangular, square and cube numbers and others including Fibonacci-type sequences and quadratic sequences,	
Understand simple arithmetic geometric progressions	
deduce expressions to calculate the nth term of linear sequences	

### Ratio, proportion and rates of change

change freely between and use related units (e.g. time, length, area, volume/capacity, mass) and compound units (e.g. speed, rates of pay, prices, density, pressure) in numerical and algebraic contexts	
use scale factors, scale diagrams and maps	
express one quantity as a fraction of another	
use ratio notation, including reduction to simplest form	
divide a given quantity into two parts in a given part : part or part : whole ratio	
express the division of a quantity into two parts as a ratio	
apply ratio to real contexts and problems including better value or best-buy problems.	
express a multiplicative relationship between two quantities as a ratio or a fraction	
understand and use proportion as equality of ratios	
relate ratios to fractions and to linear functions	
define percentage as 'number of parts per hundred'	
interpret percentages and percentage changes as a fraction or a decimal, and interpret these as a multiplier	
express one quantity as a percentage of another	
compare two quantities using percentages	
work with percentages greater than 100%	
solve problems involving percentage change, including percentage increase/decrease and original value problems, and simple interest including in financial mathematics	
solve problems involving direct and inverse proportion, including graphical and algebraic representations	
use compound units such as speed, rates of pay, unit pricing,	
compare lengths, areas and volumes using ratio notation	
understand scale factors	
make links to similarity (including trigonometric ratios)	
understand that X is inversely proportional to Y is equivalent to X is proportional to $\frac{1}{Y}$	
interpret equations that describe direct and inverse proportion	
interpret the gradient of a straight-line graph as a rate of change	
recognise and interpret graphs that illustrate direct and inverse proportion	
set up, solve and interpret the answers in growth and decay problems, including compound interest	

## Geometry and Measures

use conventional terms, vocabulary and notations	
use the standard conventions for labelling and referring to the sides and angles of triangles e.g. labelling angle ABC	
draw diagrams from written description	
use the standard ruler and compass constructions (perpendicular bisector of a line segment, constructing a perpendicular to a given line from/at a given point, bisecting a given angle); use these to construct given figures and solve loci problems, including constructing an angle of 60°.	
know that the perpendicular distance from a point to a line is the shortest distance to the line	
apply the properties of angles at a point (the angles total 180°), angles at a point on a straight line (the angles total 360°) and vertically opposite angles	
understand and use alternate and corresponding angles on parallel lines	
derive and use the sum of angles in a triangle (e.g. to deduce and use the angle sum in any polygon, and to derive properties of regular polygons)	
derive and apply the properties and definitions of: special types of quadrilaterals, including square, rectangle, parallelogram, trapezium, kite and rhombus and triangles and other plane figures using appropriate language	
use the basic congruence criteria for triangles (SSS, SAS, ASA, RHS)	
apply angle facts, triangle congruence, similarity and properties of quadrilaterals to conjecture and derive results about angles and sides, including Pythagoras' theorem and the fact that the base angles of an isosceles triangle are equal, and use known results to obtain simple proofs	
identify, describe and construct congruent and similar shapes, including on coordinate axes, by considering rotation, reflection, translation and enlargement, including fractional scale factors	
identify and apply circle definitions and properties, including: centre, radius, chord, diameter, circumference, tangent, arc, sector and segment	
solve geometrical problems on coordinate axes e.g. can you add another point to create a rhombus)	
identify properties of the faces, surfaces, edges and vertices of: cubes, cuboids, prisms, cylinders, pyramids, cones and spheres	
interpret plans and elevations of 3D shapes	
construct and interpret plans and elevations of 3D shapes	
use standard units of measure and related concepts (length, area, volume/capacity, mass, time, money etc.)	
measure line segments and angles in geometric figures, including interpreting maps and scale drawings	
be able to use bearings including the eight compass point bearings and three-figure bearings.	
know and apply formulae to calculate: area of triangles, parallelograms, trapezia;	
volume of cuboids and other right prisms (including cylinders)	
know the formulae for circumference and area of a circle,	
calculate perimeters of 2D shapes, including circles, areas of circles and composite shapes	
surface area and volume of spheres, pyramids, cones and composite solids including frustums.	
calculate arc lengths, angles and areas of sectors of circles	

apply the concepts of congruence and similarity, including the relationships between lengths in similar figures	
know the formulae used for Pythagoras' theorem and trigonometric ratios and apply them to find angles and lengths in right-angled triangles in 2D	
know the exact values of $\sin \theta$ , $\cos \theta$ and $\tan \theta$ for $\theta = 0^\circ, 30^\circ, 45^\circ, 60^\circ, 90^\circ$	
describe translations as 2D vectors	
apply addition and subtraction of vectors, multiplication of vectors by a scalar, and diagrammatic and column representations of vectors	

## Probability

be able to use tables and frequency trees to display the outcomes of probability experiments	
calculate the expected outcome of future (or given) probability events	
using appropriate language and the 0 to 1 probability scale to describe a theoretical probability	
apply the property that the probabilities of all outcomes in an event sum to 1	
apply the property that the probabilities of mutually exclusive events sum to 1	
understand that an increase in the sample size (the number of trials) will result in a more reliable result.	
understand sets and combinations of sets systematically, using tables, grids, Venn diagrams, including using tree diagrams	
understand and construct probability sample spaces for single and combined experiments with equally likely outcomes and use these to calculate theoretical probabilities	
calculate the probability of two or more events, whether independent or dependent	

## Statistics

infer properties of populations or distributions from a sample, whilst knowing the limitations of sampling	
interpret and construct tables, charts and diagrams, including frequency tables, bar charts, pie charts and pictograms for categorical data, vertical line charts for ungrouped discrete numerical data, tables and line graphs for time series data and know their appropriate use	
interpret, analyse and compare the distributions of data sets using either: <ul style="list-style-type: none"> <li>• appropriate graphical representation involving discrete, continuous and grouped data</li> <li>• appropriate measures of central tendency (median, mean, mode and modal class) and spread (range, including consideration of outliers)</li> </ul>	
know and understand the terms: primary data, secondary data, discrete data and continuous data.	
apply statistics to describe a set of data	
use and interpret scatter graphs for bivariate data; know and understand the terms for correlation: positive, negative, no, weak and strong.	
draw estimated lines of best fit and make predictions	
use a line of best fit to predict a value from the trend line (extrapolation and interpolation) whilst knowing the dangers/limitations of so doing	